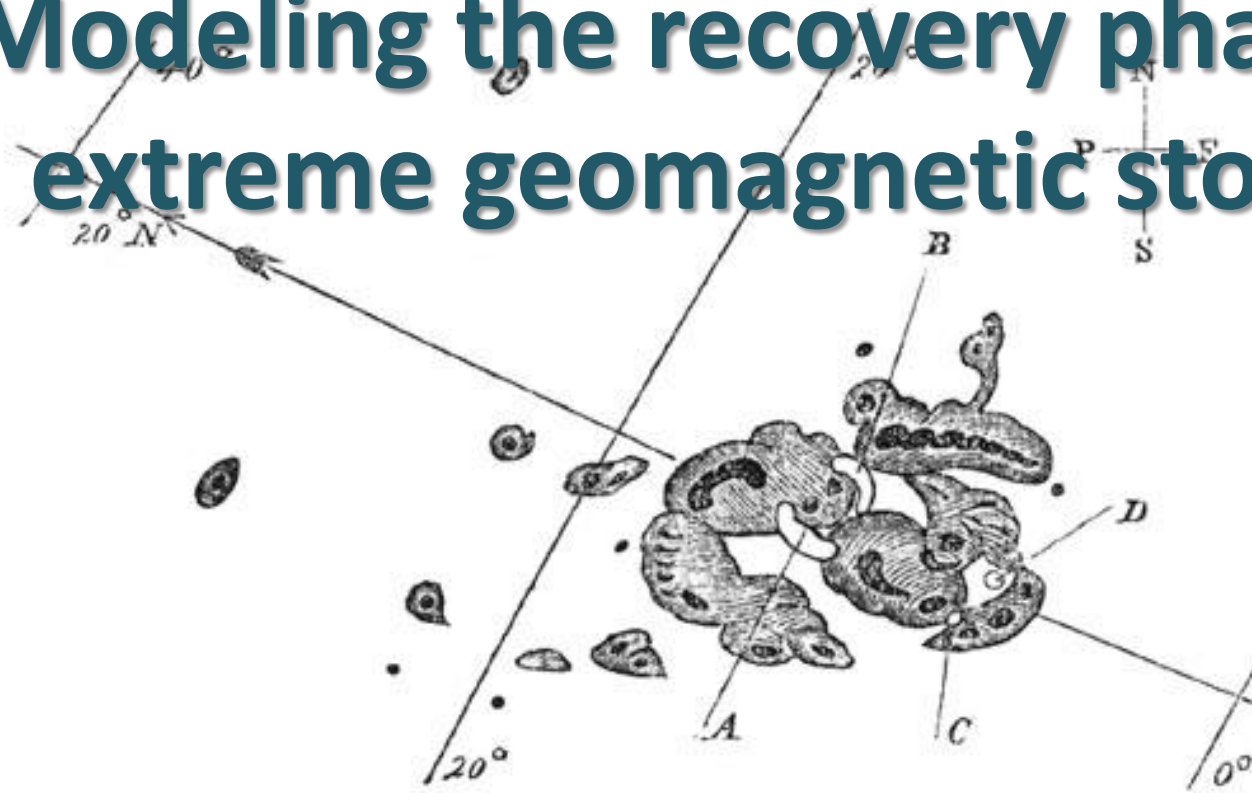


# Modeling the recovery phase of extreme geomagnetic storms



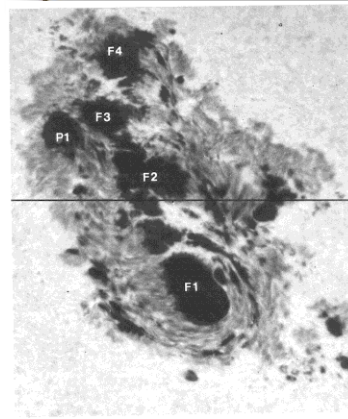
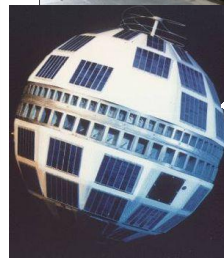
C. Cid, J. Palacios, E. Saiz, Y. Cerrato,  
J. Aguado, A. Guerrero

Space Research Group - Space Weather, Universidad de Alcalá, Spain.

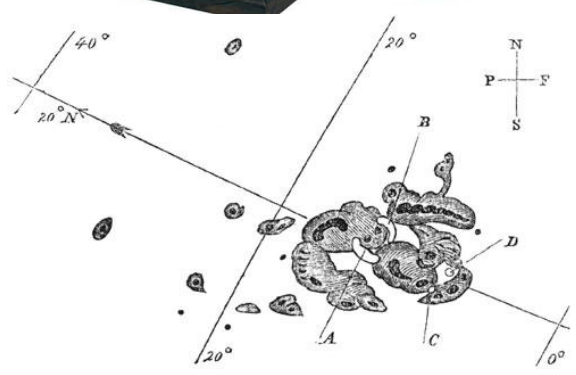
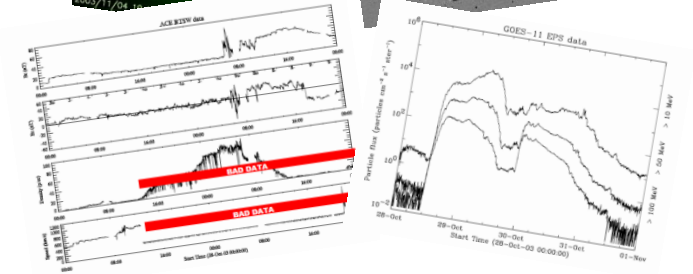
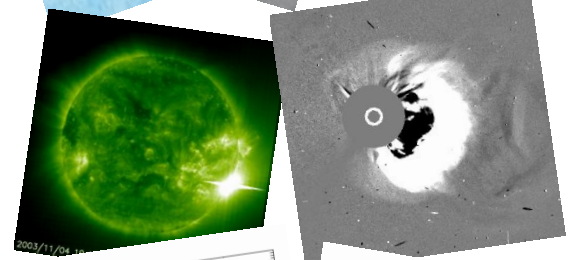
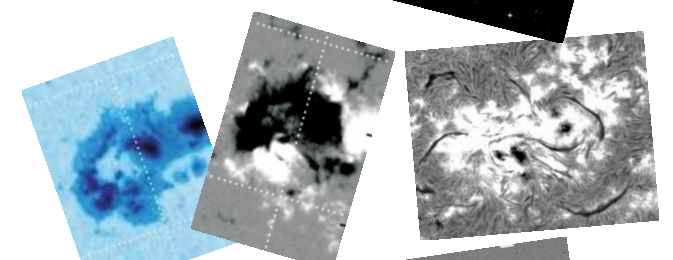
# 1859



# 1989



# 2003



# The models have also evolved

Exponential decay  
[Burton et al., 1975]

$$Dst(t) = Dst_0 e^{-t/\tau}$$

Constant

$$\frac{-(dDst / dt)}{Dst} = \frac{1}{\tau}$$

Linear

$$-(dDst / dt) \propto Dst$$

Hyperbolic decay  
[Aguado et al., 2010]

$$Dst(t) = \frac{Dst_0}{1 + \frac{t}{\tau_h}}$$

Time-dependent

$$\frac{-(dDst / dt)}{Dst} = \frac{1}{\tau_h + t}$$

Quadratic

$$-(dDst / dt) \propto Dst^2$$

# The models have also evolved -II

Exponential decay

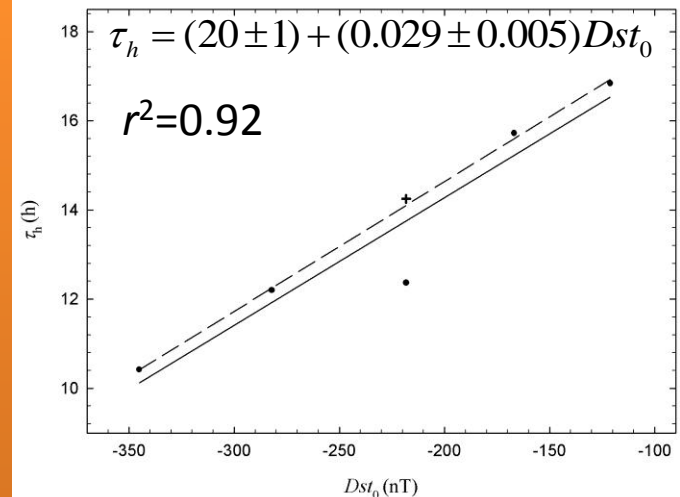
$$Dst(t) = Dst_0 e^{-t/\tau}$$

$\tau$  does not depend  
on  $Dst_0$

Two parameters

Hyperbolic decay

$$Dst(t) = \frac{Dst_0}{1 + \frac{t}{\tau_h}}$$



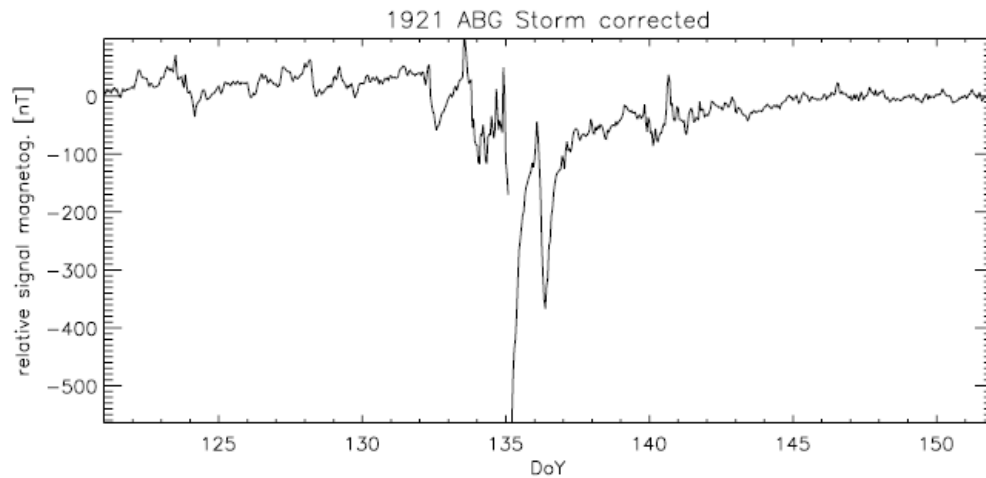
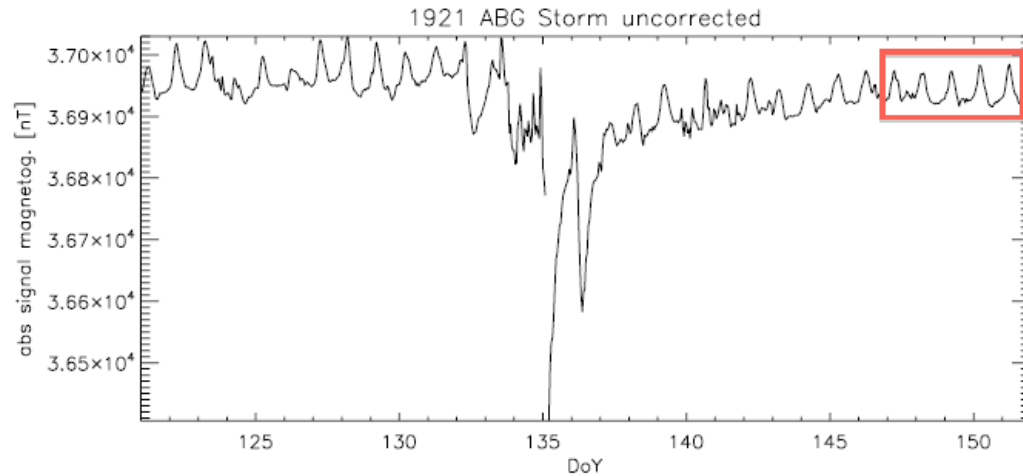
# And new models need to be validated...

## in the extreme cases!

Event #	Year	Month	Day	Observatory	H range (nT)	Geomagnetic latitude
1	1859	September	1-2	Bombay	1720	9.74
2	1921	May	13-16	Alibag	>700	9.46
3	1928	July	7	Alibag	780	9.45
4	1938	April	16	Alibag	530	9.37
5	1957	September	13	Alibag	580	9.29
6	1958	February	11	Alibag	660	9.29
7	1989	March	13	Kakioka	640	26.6

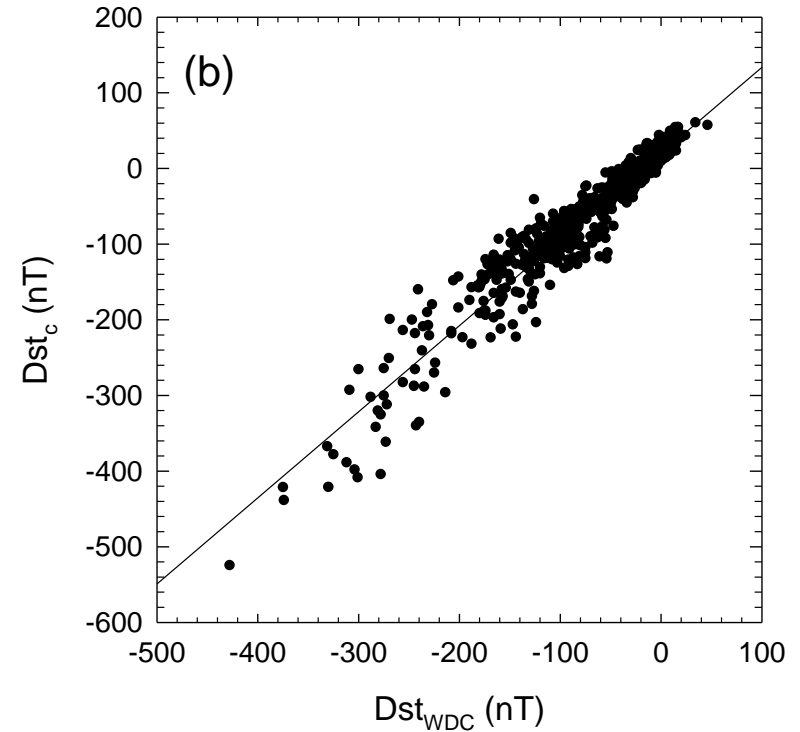
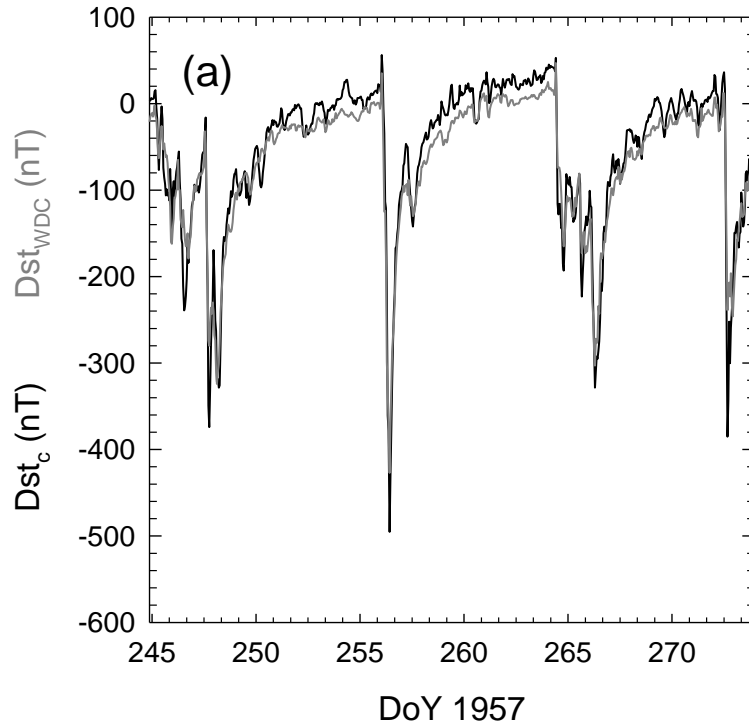
A selection of events from Tsurutani *et al.* [2003]

# Analysing individual events

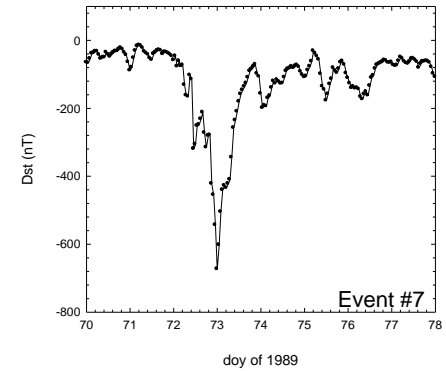
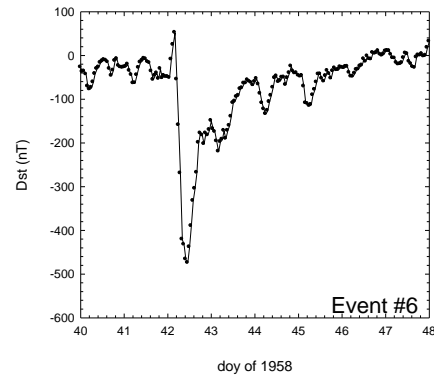
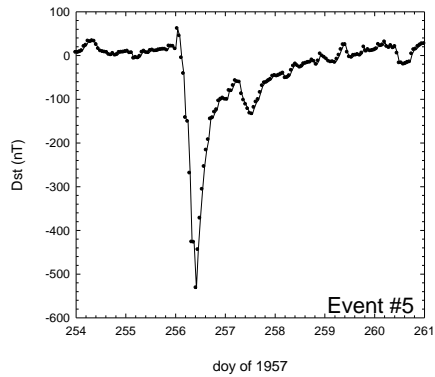
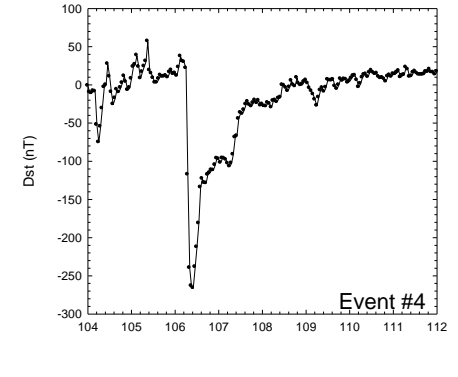
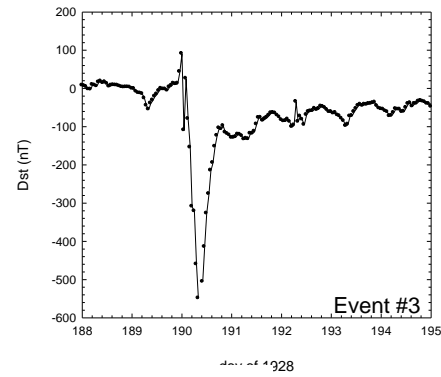
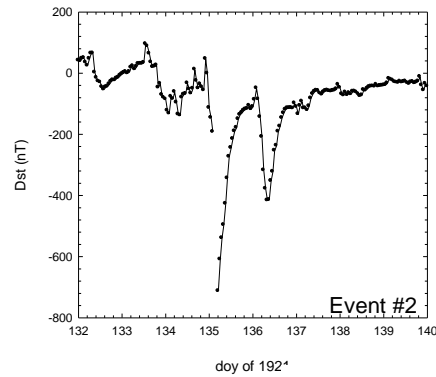
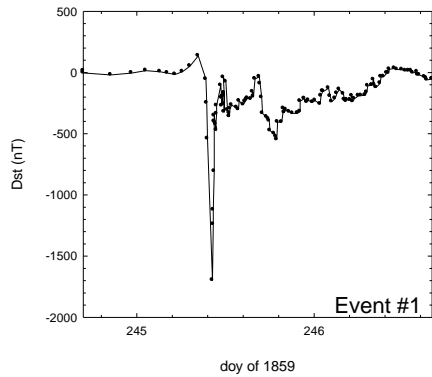


*See poster by  
Palacios et al.  
in session S12*

# LDi works fine!

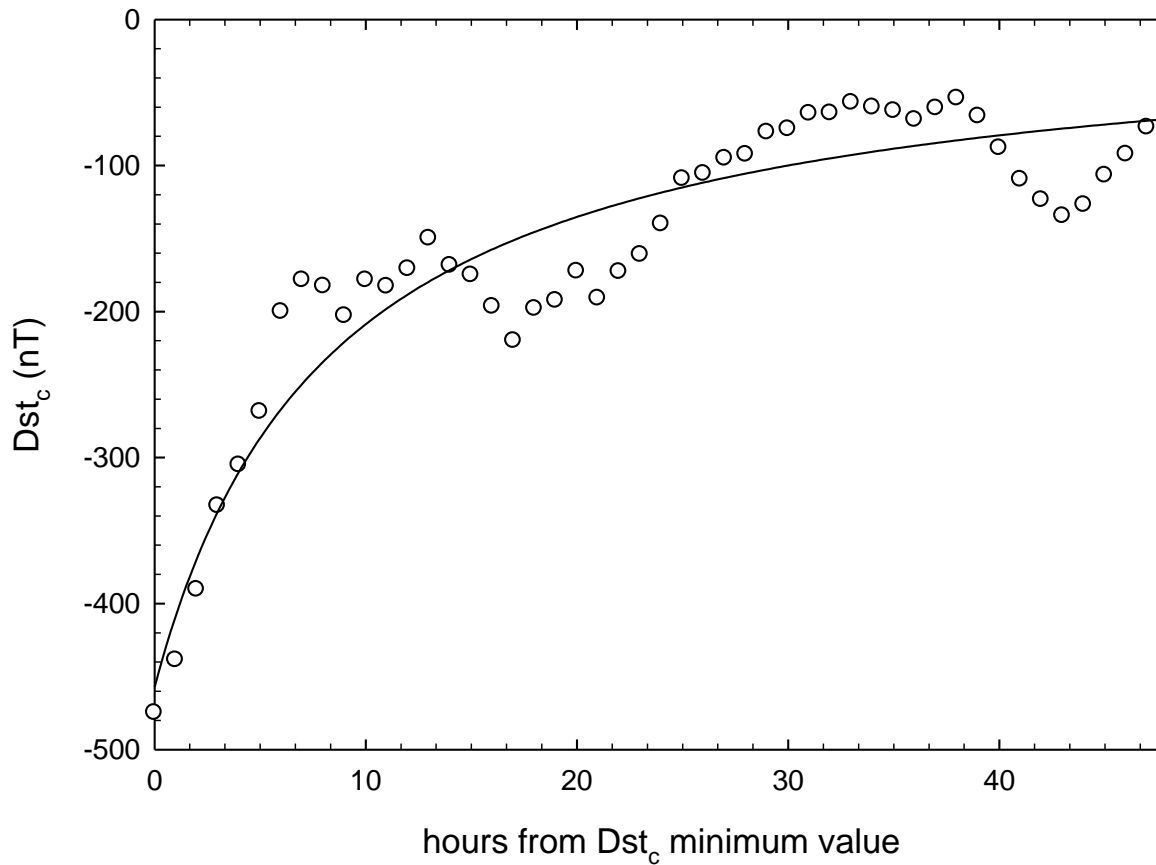


# The events ready for checking

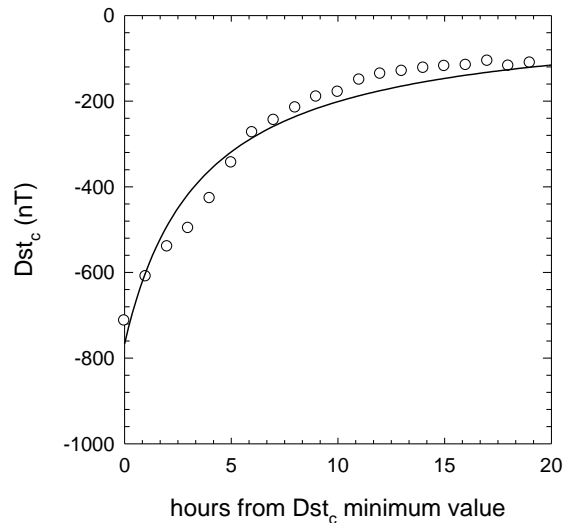
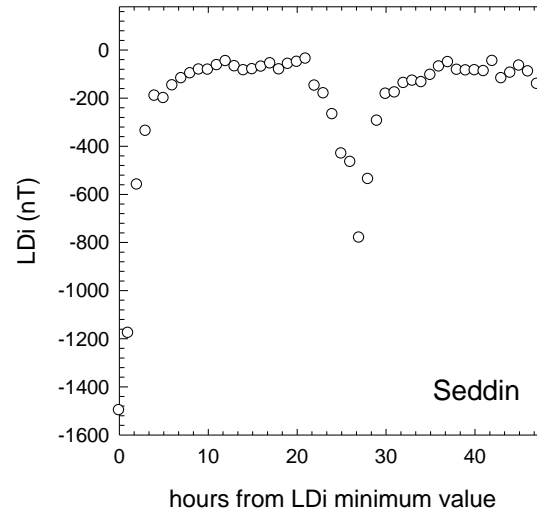
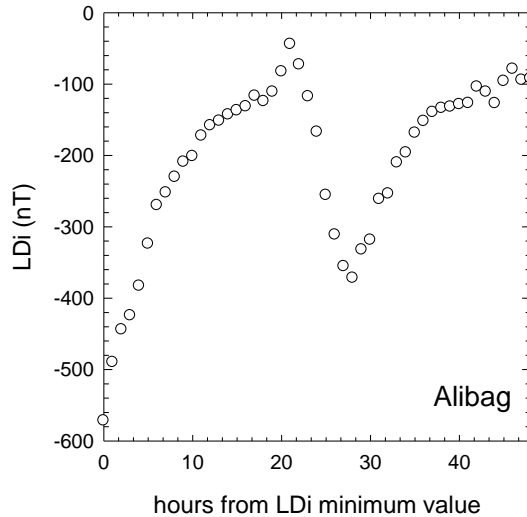




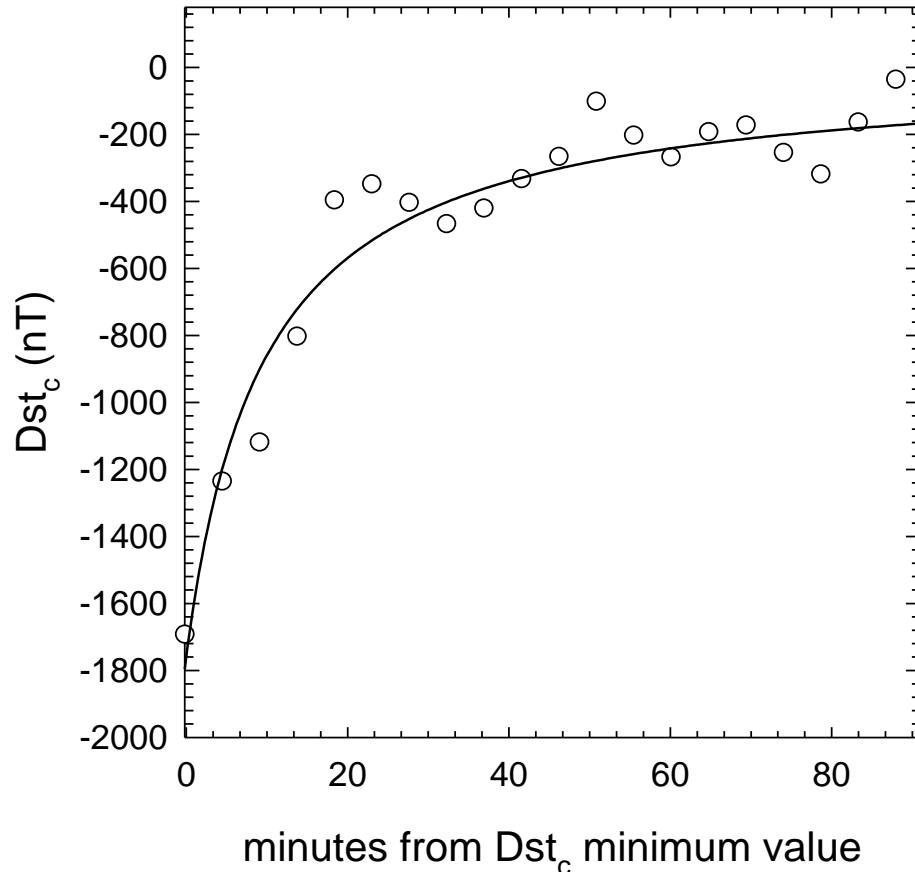
# And the results



# Problems: May 1921 event



# More Problems: Carrington event



- Double step: short interval fitted
- High resolution of computed Dst (almost SYM-H)
- Averaging to hourly resolution:

**Carrington Dst<sub>peak</sub> = 685 nT**

Comparable to the  
1989 March storm!  
(peak = 640 nT)

# The final fitting results

Event #	$t_0$ (yyyy mm dd hh:mm)	$Dst_c$ min (nT)	$\Delta t$ (h)	$\tau_h$ (h)	$Dst_0$ (nT)	$r^2$
1	1859 09 02 10:15 <sup>b</sup>	-1697	48	0.10±0.02	-1600±135	0.68
			1.47	0.14±0.02	-1753±103	0.93
2	1921 05 15 05	-713 <sup>c</sup>	48	7.27±1.70	-646±73	0.51
			20	3.55±0.34	-767±32	0.96
3	1928 07 08 10	-506	48	4.55±0.45	-585±32	0.88
4	1938 04 16 10	-263	48	6.46±0.65	-267±13	0.91
5	1957 09 13 10	-532	48	3.67±0.30	-541±22	0.93
6	1958 02 11 11	-475	48	8.40±0.90	-457±23	0.87
7	1989 03 14 00	-674	48	6.11±0.61	-688±34	0.88

Cid *et al.* [2013]

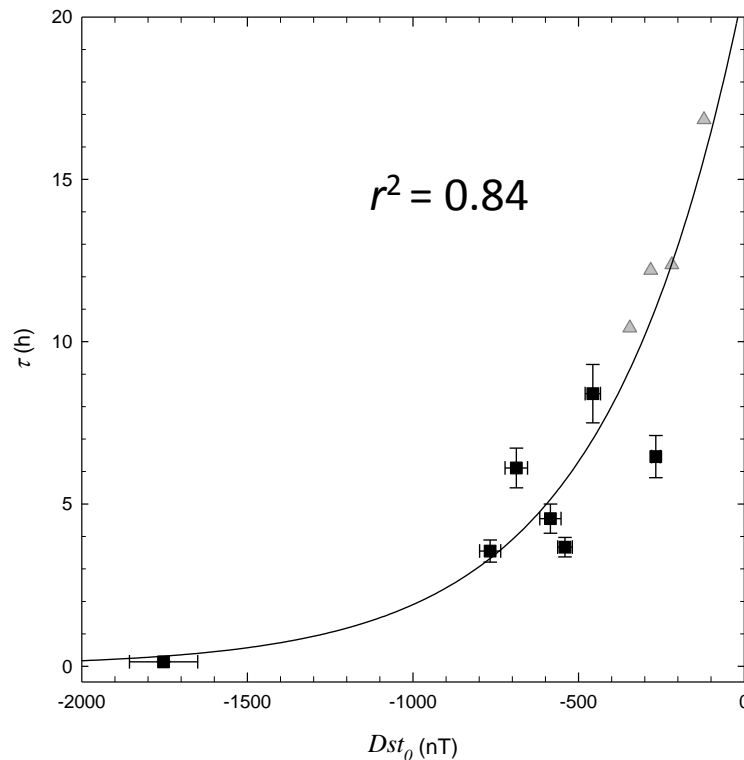
# The final fitting results

Event #	$t_0$ (yyyy mm dd hh:mm)	$Dst_c$ min (nT)	$\Delta t$ (h)	$\tau_h$ (h)	$Dst_0$ (nT)	$r^2$
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Cid *et al.* [2013]

# Both parameters are still related... but not linearly!

$$\tau_h (\text{h}) = (21 \pm 3) \exp \left[ (2.4 \pm 0.5) \times 10^{-3} Dst_0 (\text{nT}) \right]$$



*Cid et al. [2013]*

# Conclusions

- The hyperbolic decay function is able to provide by a unique continuous function and with high accuracy the recovery phase of any storm
- Although the Carrington storm is still the most intense geomagnetic storm ever recorded, it is not as extreme as usually stated